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Introduction

A frequent question posed to the RAC or posted on the RAC Forum relates to calculating the sample size “n” required in experimentation. Engineers use samples to estimate or test performance measures (PM) such as reliability, MTTF, etc. Having an adequate sample size is important, for it determines the amount of time and dollars dedicated to the effort.

The sample size used in an experiment depends, first, on the statistical distribution of the random variable (r.v.) in question (e.g., device life). Such life may be distributed Normally, a symmetric distribution whose standard deviation is usually smaller than its mean and hence induces a moderate variability. Therefore, a smaller sample size can still yield an acceptable level of certainty (or uncertainty) regarding estimates and tests.

If the r.v. life is distributed say Exponentially, a highly skewed distribution having a standard deviation as large as its mean, the situation differs. Large variances induce large variability. Hence, the r.v. can now attain either very small or very large values. This fact introduces higher levels of uncertainty in estimations, which have to be compensated by drawing larger sample sizes. Therefore, inherent variability, or variance of the r.v. under study, constitutes the second factor of importance in sample size determination.

Finally, we have the issue of the level of “confidence” in estimation problems or of the Types I and II errors1 in testing problems. To obtain higher confidence, all other factors being equal, we require wider “confidence intervals” (CI), which are usually not very useful. To reduce the width of a CI, we need to draw a larger sample. If instead of deriving a CI (estimation), we are testing, then we also need to consider the Type II error.

Summarizing, derivation of adequate sample sizes for testing or estimating a parameter requires three elements: the distribution of the r.v., its variability, and the risks of erring in the process of deriving such estimations or tests.

This START Sheet discusses and provides examples of several types of sample size derivations for location parameters. We first obtain sample sizes for interval estimation of the population using the Normal, Student t, and Exponential distributions, as well as for proportions. Then, we estimate the sample sizes for testing the mean of the Normal and of the Weibull distributions. Finally, we present examples of sample size derivation for the nonparametric (distribution-free) case. Due to its complexity, the derivation of sample sizes for estimating and testing variances will be the topic of a separate START sheet.

Sample Size for Interval Estimation of the Normal Mean

When a device life is distributed Normally, and we want to obtain an estimate of its MTTF, we base our sample size estimations on the formula for the CI for the mean (μ):

\[ \bar{x} \pm z_{\alpha/2} \frac{\sigma}{\sqrt{n}} = \bar{x} \pm H \]

In its half-length (H), which is the amount that is added and subtracted from the sample mean, the CI formula includes four elements. The four elements are, the confidence level (1 - α) desired, the random variation (σ) inherent in the Life of the device, the sample size (n) required to fulfill the requirements and the Normal Standard percentile (z_{α/2}).

The preceding probability statement says that the CI will cover the true MTTF at least 100(1-α)% of such times (e.g. 95% of the times). Let’s assume we know the standard deviation of the population. Consider now pre-establishing a fixed CI half-length of \( H = z_{α/2} \times \sigma / \sqrt{n} \), about the true MTTF, for a pre-specified

---

1 We commit a Type I Error when we decide that the alternative hypothesis (H₁) is true, when in fact the null (H₀) is true (e.g. assume that the mean is \( \mu_1 \), when in fact it is \( \mu_0 \)).

We commit a Type II Error when we decide that the null hypothesis (H₀) is true, when in fact the null (H₀) is true (e.g. assume that the mean is \( \mu_0 \), when in fact it is \( \mu_1 \)).
confidence level (1-α). Such equation H defines all our needs. After some algebraic manipulations, we obtain the sample size:

$$n = \frac{(z_{α/2}/σA)2}{H^2}$$

To illustrate this with a numerical example, assume that a device life has a Normal distribution, and that the standard deviation σ is known to be 8.6 units of time. Assume that we want to derive a 95% CI for the MTTF with a "precision" H of two time units (i.e., 95% of the times, MTTF estimates will be two units or less, away from the true but unknown MTTF of the device Life). Then, we would require a sample size of:

$$n = \frac{1.96^2 \times 8.6^2}{2^2} = 71.03 \approx 72 \text{ observations}$$

Assume now that the device Life has a Normal distribution, but the standard deviation σ is unknown, but estimated (s) from a pilot sample, prior experience, or using other means. Now we need to use an iterative process, using the Student t distribution:

$$n = \frac{t_{α/2,n-1} \times s}{H} = \frac{(t_{α/2,n-1})2 \times s^2}{H^2}$$

The basic line of thought is exactly the same as before, except that now we use Student t instead of the Normal percentile. This introduces an interesting twist, since the t percentile requires knowledge of the Degrees of Freedom (DF), which in turn depends on the sample size (DF = n - 1). However, the sample size “n” is not known, because that is precisely what we are looking for with this procedure.

The solution is to set an initial, arbitrary sample size “n.” Then, using the t percentile for these DF, we calculate a resulting sample size n’. Then, we compare n with n’ and see if they agree or not. If they do, we stop. If not, we let n’ determine the new DF and iterate.

We illustrate this method with the previous numerical example. But now assume that the standard deviation is unknown but we have an estimate of 8.6. Define an initial n = 20:

$$n’ = \frac{(t_{0.05/2,20-1})2 \times 8.6^2}{2^2} = \frac{2.093^2 \times 73.96}{4} = 80.998 \approx 81$$

Since n’ = 81 differs from 20, we must iterate the calculations, using DF = 81 - 1 = 80:

$$n’ = \frac{(t_{0.05/2,80-1})2 \times 8.6^2}{2^2} = \frac{1.99^2 \times 73.96}{4} = 73.22 \approx 74$$

Proceeding this way, we arrive to the final value of n = 75, higher than the value n = 72, obtained for the case where σ was known. Notice how we pay the price of drawing three additional observations to compensate for the lack of information about σ.

Finally, consider the case of Life with a Normal distribution, when the standard deviation σ is known, or is unknown and estimated by “s.” Suppose that, instead of deriving a CI, we require the sample size n for a hypothesis test. Then, in addition to Type I error α, we must also consider Type II error β. Such error yields a difference of δ = μ₀ - μ₁.

The sample size is obtained by considering a system of two equations, derived from the Operating Characteristic function (5), and assuming the two error probabilities α and β are given. Solving the resulting system of two equations yields the required sample size:

$$n = \frac{z_{α} + z_{β})^2}{δ^2}$$

In the previous example, assume we now want the sample size n for a test that detects a difference of two units (δ = 2) in MTTFs with errors α = 0.05 and β = 0.1, when σ = 8.6:

$$n = \frac{z_{0.05} + z_{0.1})^2}{2^2} = \frac{1.65 + 1.28 \times 8.6^2}{2} = 158.7 \approx 158$$

By adding the extra requirement that we err if we accept a MTTF μ₁ further than 2 units away from the true μ, the sample size n has increased to 158. Error β can now be at most 10% yielding z_β = z_0.1 = 1.28. We have discussed these derivations in the START on OC Functions (5). The interested reader will find more details and numerical examples in that reference.

**Sample Size for Interval Estimation of a Proportion**

A frequent query submitted to RAC deals with determining the sample size required for estimating the true proportion defective “p,” or the true reliability “R” of a device, for a given Mission Time.

These two cases are, conceptually from a statistical point of view, handled the same. For, if we know the reliability required for a mission time “T,” or we can estimate it, then a device failure to meet such reliability requirement is equivalent to it being “defective.” Hence, the unreliability “p” is now P {Device Life < T} = p = 1 - R and, from the CI formula:

$$p \pm z_{α/2} \sqrt{\frac{p(1-p)}{n}} = p \pm H$$
If, as before, we pre-establish the “precision” H, and the “confidence” (1-α) then, after some algebra, we obtain the formula for the sample size “n” required to fulfill these:

\[ n = \left( \frac{z_{\alpha/2}}{p(1-p)} \right)^2 \]

To illustrate the percent defective (PD) calculations, assume we want to obtain the sample size required to estimate, with an 80% confidence (α = 0.2) the PD in a production lot. Assume a precision “H” of, at most, 3% (e.g. the maximum distance we want such estimate “p” to be from the true, but unknown, lot PD, either by excess or by defect). We say: H = 0.03, with confidence (1-α) = 0.8. We need, as with the Student t case, a preliminary estimate of the true lot PD parameter. We can obtain such estimate from a pilot survey or historical data (or, worst case, by assuming p = 0.5). Let, in our example, this estimate be p = 0.05. Then, the sample size required is:

\[ n = \left( \frac{z_{0.025}}{\sqrt{0.05(1-0.05)}} \right)^2 = (1.28/0.03)^2*0.05*0.95 = 86.47 \approx 87 \]

Hence, a sample of n = 87 yields an estimate of PD “p”, such that 80% of the time, it is not further than 3% from the true but unknown PD. The procedure is valid when np and n(1-p) are greater than 5. Our example is borderline, since np = 87 × 0.05 = 4.35 ≈ 5.

Assume we want instead an estimate of device reliability, for a Mission Time T, and we know it is somewhere around 0.95. If the reliability point estimate is: R = 1 - 0.5 = 0.95, then the probability of failure in time T is p = .05. Also assume a “precision” H = 0.03 (i.e. no further than 0.03 above or below 0.95) with at least 80% “confidence.” Then, we perform the same calculations above (p = 1 - R) obtaining the same sample size n = 87.

An alternative method consists of using Binomial nomographs, which can be found in the References. Nomographs are very useful in determining sample sizes when, if instead of a CI, we derive a hypothesis test. Then, in addition to Type I error α, we must also consider Type II error β, which comes from accepting a bad hypothesis.

**Sample Size for Estimating the Exponential Mean**

We know, from Reference 4, that if “n” devices have lives \( X_i \) \( i = 1 \), … , n, distributed as Exponential with MTTF = μ, then the statistic \( 2T/\mu \) (where \( T = \Sigma X_i \)) is distributed as Chi Square (\( X^2 \)) with DF = 2n. From this we get the 100(1-α)% CI, say 95%, for MTTF (μ):

\[ n = \left( \frac{z_{\alpha/2}}{\sqrt{0.05(1-0.05)}} \right)^2 \]

As in the Normal case, we want a “precision” or maximum distance “r” from either CI limit (2T/\( X^2 \)) to the real (unknown) value of MTTF (μ). But now, we express this as the ratio τ:

\[ \tau = \frac{\mu - 2T}{X^2_{2n,1-\alpha/2}}; \text{or; } \tau = \frac{2T}{X^2_{1-\alpha/2}} - \mu \]

Following (1), we denote \( C = X^2_{2n,\alpha/2} \) and \( D = X^2_{(1-\alpha)/2,2n} \). We solve the preceding system of two equations for variables C, D, and τ. After some algebra manipulations, we obtain:

\[ \tau = \frac{C - D}{C + D} \Rightarrow \tau = \frac{X^2_{2,\alpha/2}}{X^2_{2,1-\alpha/2}} = 1 + \tau \]

Therefore, to obtain the adequate DF, we only need to inspect the Chi Square Tables, finding the ratio that fulfills the conditions, for confidence (1-α) and precision τ. For example, assume we seek the sample size requirement for a 90% CI for the MTTF, with a precision of 45%. Then, 1-α = 0.9, α = 0.1, α/2 = 0.05, τ = 0.45 and ratio C/D is:

\[ C = X^2_{0.95,24} = 36.415 \]
\[ D = X^2_{0.05,24} = 13.848 \]

Hence: 2n = 24 ⇒ n = 12

When the sample size n required is large, we can use the Normal approximation to the Chi Square distribution: \( z = \sqrt{2X^2_{\alpha/2}} - \sqrt{2(2n-1)} \). With some algebra, we then obtain:

\[ \left( \frac{\sqrt{4n-1} + z_{\alpha/2}}{\sqrt{4n-1} - z_{\alpha/2}} \right)^2 = 1 + \tau \Rightarrow n = \frac{1}{4} \left( \frac{1}{2} \right)^2 \left[ \frac{1}{\sqrt{1 + \left( \frac{1}{\tau} \right)^2} - 1} \right]^2 \]

For example, assume we now seek the sample size requirement for a 95% CI for MTTF, with a precision of 20%. Then, 1-α = 0.95, α = 0.05, α/2 = 0.05, τ = 0.2. The result is:

\[ n = \frac{1}{4} + \left( \frac{1}{2} \right)^2 \left[ \frac{1}{0.05} \left( \frac{1}{0.05} + \sqrt{0.025} - 1 \right) - 2 \right] \]

\[ = 0.25 + 0.95^2 \left( \frac{5 + \sqrt{25} - 1}{0.2} \right) - 0.5 = 93.8 \]

To verify this, we calculate the ratio of the two Chi Squares, with DF = 2n ≈ 188:

\[ \frac{X^2_{0.975,188}}{X^2_{0.025,188}} = 227.863 \approx 1.499 \approx 1 + \tau = 1 + 0.2 = 1.2 \]

\[ = 1.5 \]


Hence, a 95% CI for the Exponential MTTF of the device lives, with a precision of 20% of the true MTTF, i.e. \( \tau = 0.2 \), would require drawing about 94 observations.

**Sample Size Requirements for Testing the Weibull Mean**

Sometimes we need the sample size requirements for testing, instead of for estimating parameters. We will illustrate this situation for the Weibull distribution. Assume we need the sample size “n” to test the Weibull Mean Life “m,” when shape parameter \( \beta \) is known, and Types I and II errors (producer and consumer risks), device reliability R and test time T are given.

Weibull also involves a scale or characteristic life parameter \( \eta \) (now a “nuisance” parameter) that we, of necessity, need to substitute out of our equations.

We follow the algorithm described in (1). Using the Weibull density \( f(x) \), the cumulative distribution \( F(x) \), the mean life “m,” and the Reliability \( R(x) \):

\[
f(x) = \frac{\beta}{\eta} x^{\beta-1} \exp\left(-\left(\frac{x}{\eta}\right)^\beta\right) \quad \text{and} \quad F(x) = 1 - \exp\left(-\left(\frac{x}{\eta}\right)^\beta\right)
\]

\[
R(x) = P(X \geq x) = \exp\{-x/(\eta)^{\beta}\}
\]

We can construct a Test Plan \((n, c)\) that yields a sample size “n” to test the Weibull Mean Life “m,” when shape \( \beta \) and error \( \alpha \) and \( \beta \) are known.

To achieve this, we assume that the r.v. “number of failures in test time T,” denoted “x” can be approximated by a Binomial \((n, p)\) distribution. The parameters are “n,” the number of trials or devices placed on test, and “p,” the probability of having a device failure at any trial:

\[
p = F(T) = 1 - R(T) = 1 - \exp\{-(T/\eta)^{\beta}\}
\]

We define a hypothesis test for device mean life “m”, that fulfills Types I and II errors \( \alpha \) and \( \beta \), yielding Confidence (1-\( \alpha \)) and Power (1-\( \beta \)). The two hypotheses \( H_0: m = m_i \), for \( i = 0,1 \) were originally based on the Weibull mean. However, they are now converted, after some algebra, into hypotheses \( H^*: p = p_i \), for \( i = 0,1 \), based on Binomial parameter “p”:

\[
p_i = 1 - \exp\left(-\left(\frac{m_i}{T}\right)^\beta \times \left(\frac{1}{\beta + 1}\right)\right) \quad \text{for} \quad i = 0,1
\]

Since shape \( \beta \) is known, reliability \( R(T) = 1 - p \) is only a function of \( T/m \), the known test time “T” and the hypothesized Weibull mean “m.” We can then establish a system of two Binomial equations that fulfill the required Types I and II errors (or risks) of the problem:

\[
\sum_{x=0}^c \binom{n}{x} p_0^x (1-p_0)^{n-x} = 1 - \alpha; \quad \text{and} \quad \sum_{x=0}^c \binom{n}{x} p_1^x (1-p_1)^{n-x} = \beta
\]

Solving this system of two equations, we obtain the appropriate values of “c” and “n” for the problem. This is the least preferred method, given its computational difficulties and trial-and-error approach to obtaining simultaneously “n” and “c.” We still use it (once “n” and “c” are obtained by one of the other two methods described below) but only to check their accuracy.

The alternative includes implementing a graphical method for obtaining such “n” and “c” values. It is similar to the method for obtaining an acceptance plan from an OC curve (5). Let’s explain its use through a numerical example.

Say we seek the sample size “n” required to test that the mean “m” of a Weibull life is 5000 hours, versus that is 1000 hours. The time T available for testing each device is only 500 hours, and both risks \( \alpha \) and \( \beta \) are 0.01. The Weibull shape parameter is known to be \( \beta = 2 \). We first need to calculate the two \( p_i \), for i = 0,1, from the equations given above:

\[
p_0 = 1 - \exp\left(-\left(\frac{500}{5000}\right)^2 \times \left(\frac{1}{2 + 1}\right)^2\right) = 1 - 0.9922
\]

\[
p_1 = 1 - \exp\left(-\left(\frac{500}{1000}\right)^2 \times \left(\frac{1}{2 + 1}\right)^2\right) = 1 - 0.8217
\]

Then, we place the two \( p_i \) values obtained on the left scale of the Acceptance Plan graph (Refs. 1, 5, 7) in Figure X. Probabilities for Confidence (1-\( \alpha \)) = 1 - 0.01 = 0.99 and Type II Error \( \beta = 0.01 \) are placed on the right hand scale of the Acceptance Plan graph.

Finally, we draw the two connecting lines for these pairs of points, as done in Figure 1, and find values \( n = 46 \) and \( c = 2 \), in the chart margins. These values were obtained by projecting the intersection point of these two lines, in the margin scales.

We can then check the resulting n and c values, by substituting them, jointly with the values \( p_i \), for i = 0,1 and \( \alpha \) and \( \beta \), in the above Binomial equations. That is:
\[ \sum_{x=0}^{c} \binom{n}{x} p_0^x (1-p_0)^{n-x} = 1 - \alpha = 0.99; \]
\[ \sum_{x=0}^{c} \binom{n}{x} p_1^x (1-p_1)^{n-x} = \beta = 0.01 \]

There exists however, a third alternative or method for this problem, consisting in certain approximations that allow us to avoid the above graphical procedures. When sample size "\( n \)" is large, say greater than 20, the r.v. “\( x \)" approaches the Normal, with \( \mu = np \) and \( \sigma^2 = np(1-p) \). We can then, using the same two hypothesized \( p_i \) for \( i = 0,1 \), and the two errors or risks \( \alpha \) and \( \beta \) given above, establish a system of two simultaneous equations to find adequate values for both \( n \) and \( c \):

\[
\frac{c - np_0}{\sqrt{np_0(1-p_0)}} = z_\alpha; \\
\frac{c - np_1}{\sqrt{np_1(1-p_1)}} = -z_\beta.
\]

Here, the \( z_\alpha \) are the Normal Standard percentiles for probability \( \alpha \). Solving this system for "\( n \)" and "\( c \)”, we obtain the equations

\[
n = \left[ \frac{z_\alpha \sqrt{p_0(1-p_0)} + z_\beta \sqrt{p_1(1-p_1)}}{p_1 - p_0} \right]^2 \\
\text{and } c = np_0 + z_\alpha \sqrt{np_0(1-p_0)}
\]

For the same numerical example given before, and substituting proportions \( p_0 = 0.0078 \) and \( p_1 = 0.1783 \) in the above equations, we obtain the adequate values \( n \) and \( c \):

\[
n = \left[ \frac{z_{0.01} \sqrt{p_0(1-p_0)} + z_{0.01} \sqrt{p_1(1-p_1)}}{p_1 - p_0} \right]^2 \\
= \left[ \frac{2 \sqrt{0.0078(1-0.0078) + 0.1783(1-0.1783)^2}}{0.1783 - 0.0078} \right]^2 \\
= 41.3 \approx 42 \\
c = np_0 + z_{0.01} \sqrt{np_0(1-p_0)} \\
= 42 \times 0.0078 + 2.326 \times 0.0078 = 1.66 \approx 2
\]

We can verify how the three pairs of values \((n, c)\), obtained by these three alternative methods, are very close, as expected.

**Sample Size and Nonparametric Estimation for Zero Failures**

In the previous section, we discussed the case where we assumed that the device life is Weibull. Sometimes, we cannot (or do not want to) assume a specific distribution. In such cases, we must use a nonparametric approach (also known as distribution free, since no distribution is specified). However, there is a cost of not specifying a distribution: we now have to define the test length as equal to the Mission Time (not less, as we did above).

We again place “\( n \)” random, identically distributed, and independent items on a life test, now for the pre-specified Mission Time length “\( T \)” Each item will either fail or pass the test of length \( T \). Hence, each item on test is an independent Bernoulli trial and the r.v. number of observed failures “\( x \)”, out of “\( n \)” trials, is distributed Binomial. The failure probability is \( p = 1 - R \), where \( R \) is the probability that any item survives mission time \( T \). Using the Binomial tables and the required reliability \( R \), we calculate the sample size “\( n \)” that provides the “Confidence” \((1 - \alpha)\) required in the problem statement.

For example, to demonstrate a reliability \( R = 0.95 \), with a Confidence \( 1-\alpha = 0.9 \), for a Mission Time of \( T \) hours and no failures, we place “\( n \)” devices on a test of length \( T \). Each device can fail the test with probability \( p = 1 - R = 0.05 \). Since zero failures implies that all “\( n \)” devices “survive”, we search the Binomial tables for a convenient sample size “\( n \)” This “\( n \)” must yield zero failures \((c = 0)\), or equivalently twenty survivals, with Confidence \( 1- \alpha = 0.9 \). The Binomial \((n, p)\) equation is then:

\[
\text{Prob(Obtaining, } c \text{ or Less Failures)} = \sum_{x=0}^{c} \binom{n}{x} p^x (1-p)^{n-x}
\]

Since the required Confidence \( 1 - \alpha = 0.9 \) and zero failures is \( c = 0 \), we have:

\[
P \{ \text{Observing NO failures} \} = (1-p)^n = R^n = (0.95)^n = \alpha = 0.1 \\
\Rightarrow (0.95)^{45} = 0.0994 \approx 0.1, \text{ for } n \approx 45.
\]

Hence, a sample of size \( n = 45 \) yields a confidence close to \( 0.9 \), of finding zero failures \((c=0)\) in a life test of Mission Time \( T \), when the reliability for this mission time \( T \) is 0.95.

However, searching the Binomial \((n,p)\) tables for a suitable “\( n \)” can be a tedious and time consuming task. We can instead use an equivalent equation, derived from such Binomial probability for the Confidence, for the case of zero failures \((c=0)\) or twenty successes:
\[
\sum_{x=0}^{c} C_{x}^{n} p^{x} (1-p)^{n-x} = 1 - \text{Confidence} = \alpha
\]

For \( c = 0 \) \( \sum_{x=0}^{c} C_{x}^{n} p^{x} (1-p)^{n-x} = (1-p)^{n} \)

\[
= \text{Exp} \{ n \text{Log}(1-p) \} = 1 - \text{Confidence} = \alpha
\]

Taking Logarithms on both sides, noticing that \( p = 1 - R \), and after some algebra, we obtain:

\[
n = \frac{\text{Log}(1 - \text{Confidence})}{\text{Log}(1-p)} = \frac{\text{Log}(\alpha)}{\text{Log}(R)}
\]

For example, applying this formula to the immediately preceding example, we obtain:

\[
n = \frac{\text{Log}(0.1)}{\text{Log}(0.95)} = \frac{-1.0}{-0.2227} = 44.89 \approx 45
\]

The results, obtained using the Binomial and the Logarithm formula, are close because both methods are totally equivalent. However, the second result (formula) is easier and faster to obtain than the first one (trial and error).

Summarizing, we first establish the problem requirements regarding the desired (1-\( \alpha \)) confidence and acceptable reliability \( R \). Then, we calculate the sample size \( n \) that satisfies these requirements. Such sample size \( n \) can then be used to estimate the reliability \( R \), with the desired confidence. The life test must be of length equal to Mission Time \( T \).

**Conclusions**

The theory for determining the sample size that meets a testing or estimation requirement is extensive and complex. Such theory is driven by the type of parameter we want to estimate or test (i.e. location, scale, or shape) and by the distribution of the sampling statistic we use to implement the hypothesis test or to obtain the estimation.

In this START Sheet, we have discussed the problem of estimating and testing some location parameters (mean, proportion) for the Normal, Exponential, and Weibull distributions, and for distribution-free (nonparametric) situations. Our objective has been to illustrate the logic and the statistical thinking behind the derivation of such sample sizes. A better understanding of this logic may help practicing engineers to better implement such procedures.

We have only discussed a few of the most widely used cases. There are many other situations of interest. For a more extensive and in-depth treatment of this subject, the reader is referred to Chapter 13, pages 699 to 776, of Reference 1.

An assessment of the complexity of these derivations may be provided by the fact that the referred Chapter 13 is the last one of this extensive, two-volume reliability handbook. However, the manifold advantages that deriving an adequate sample size for our problem provides in terms of savings in time and effort, far outweighs its theoretical complexities.

**Further Reading**

5. OC Functions and Acceptance Sampling Plans. Romeu, J. L. RAC START. Volume 12, Number 1.

**About the Author**

Dr. Jorge Luis Romeu is the founder and director of the Juarez Lincoln Marti International Education Project, that provides books and faculty workshops to Iberoamerican institutions of higher education. JLM Project is the sponsor of the QR&CHI Project. Romeu has over 30 years of statistics and operations research experience in consulting, research, and teaching.

As a consultant, Romeu has worked for both manufacturing and agriculture. He has worked in simulation modeling and data analysis, in software and hardware reliability, in software engineering, and ecological problems.

Romeu has taught both undergraduate and graduate industrial statistics, operations research, and computer science in several American and foreign universities. He is currently a Research Professor and an Adjunct Professor of Industrial Statistics and Quality Engineering, with Syracuse University.
Romeu has been a senior reliability and industrial statistics advisor for IIT Research Institute/IITRI, Alion and Quanterion. He has written a book on *Statistical Analysis of Materials Data*, designed and taught short reliability and statistics courses for practicing engineers, and written a series of articles on statistics and data analysis for the AMPTIAC and RAC.

For his work in education and research and for his publications and presentations, Romeu was elected Chartered Statistician Fellow of the Royal Statistical Society, Full Member of the Operations Research Society of America, and Fellow of the Institute of Statisticians. He has received several international awards, including five Fulbright and one Department of State Senior Specialist assignments, in Mexico, Ecuador and the Dominican Republic. He has also held assignments in Spain and Latin America and is fluent in Spanish, English and French.

Romeu is a Senior Member of the American Society for Quality and holds Quality and Reliability Engineering certifications. He is Chair of the Syracuse Section of ASQ. Romeu is a member of the American Statistical Association and its Industrial Statistics Sections. He is Associate Newsletter Editor for SPSS/QP. He is also a member of the Inter American Statistical Association.

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The Quality, Reliability and Continuous Improvement Institute (QR&CII) is a Non-Profit, Public Service Affiliate of the Juarez Lincoln Marti (JLM) International Education Project (http://web.cortland.edu/matresearch). The CR&CII serves as an Industrial Education focal point for individual efforts of individuals seeking to improve their professional education, on their own, by reading at their pace, in their time. To this end the QR&CII develops and published tutorials in applied industrial statistics. QR&CII also locates and evaluates tutorial information on statistical techniques and methods, data analyses, application guides, statistical software packages, public and private training courses, and consulting services, and makes them available to the public.